

Self-reinforcing effects between housing prices and credit.

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Abstract

The financial crisis has brought the interaction between housing prices and household borrowing into the limelight of the economic policy debate. This paper examines the nexus of housing prices and credit in Norway within a structural vector error correction model (SVECM) over the period 1986q2-2008q4. The results establish a two way interaction in the long run, so that higher housing prices lead to a credit expansion, which in turn puts an upward pressure on prices. Interest rates influence housing prices indirectly through the credit channel. Furthermore, households' expectations about the future development of their own income as well as in the Norwegian economy has a significant impact on housing price growth. Dynamic simulations show how shocks are propagated and amplified. When we augment the model to include the supply side of the housing market, these effects are dampened.

Keywords: *Housing prices, household borrowing, financial accelerator, SVECM, dynamic simulations*

JEL classification: *C32, C52, E44, G21, G28*

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1 Introduction

The world wide financial crisis that originated with the US sub-prime crisis of 2007 has highlighted the importance of the interplay between financial markets and the real economy. A great number of factors contributed to the current crisis, see IMF (2009), Hubbard and Mayer (2009) and Acharia and Schnabl (2009). However, it seems to be widely agreed that it was primarily an unsustainable weakening of credit standards that induced the US mortgage lending and housing bubble. Other countries with more stable credit conditions were mainly affected through the international financial linkages, *e.g.* European banks incurring heavy losses on securities tightly connected to the US mortgage market in the wake of the meltdown. In those countries, as Duca et al. (2010) emphasize, any overshooting of construction and housing prices owed more to traditional housing supply and demand factors.

However, there is a two-way direction of causation since imbalances in the housing market oftentimes have threatened the stability of the financial sector. In the past there have been numerous episodes where falling housing prices have preceded financial crises, as Koetter and Poghosyan (2010) point out. They also argue that, due to decentralized trading with imperfect information and high transaction costs on the one hand and slow supply responses due to construction lags and limited land availability on the other, sustained deviations from the long run equilibrium will occur more frequently in the housing market than in the financial markets.

In the housing market the amount of credit made available by lenders depends on the net worth of the debtors. Due to imperfections and informational asymmetries in the credit markets, a prospective borrower is usually granted a loan only by putting up collateral. In the models developed by Kiyotaki and Moore (1997) and Bernanke and Gertler (1989) shocks to the real economy are amplified through the credit market by altering the value of borrowers' net worth.

This so-called *financial accelerator*¹ mechanism offers an explanation to the housing market fluctuations. First, higher housing prices increase the amount of credit needed to finance a given housing purchase. Thus, we would expect higher property valuations to put an upward pressure on the demand for credit. Second, most housing loans are secured by the property itself. An increase in housing prices raises the value of the housing capital, which feeds into a greater net worth for the household sector. By increasing the net worth and thus the value of the collateral, higher housing prices will increase their borrowing capacity. At the same time, higher property valuations make banks' assets less risky, as the increased value of the collateral pledged reduces the likelihood of defaults on existing loans, which may motivate the banks to expand their lending.

That said, most housing purchases are financed by credit, and changes in household borrowing are expected to affect housing prices. The potential self-reinforcing mechanism that works between these markets makes it important to study from the perspective of financial stability, and it constitutes a main reason why central banks commonly assess financial sector vulnerability by monitoring both property prices and credit growth. The close relationship between the evolution of property prices and credit aggregates has been a focal point in the policy-oriented literature, see *e.g.* Borio et al. (1994).

¹The term was coined in Bernanke and Gertler (1995), see also Bernanke et al. (1999).

In this paper, we analyze the interaction between housing prices and credit in Norway. The paper contributes to the literature in several ways. First, we use a multivariate cointegration analysis, while most existing studies rely on single equation methods. We expect to find (at least) two cointegrating vectors and the system analysis is important for both identification and for estimation efficiency. The disposable income for the household sector is included as a third endogenous variable in the VAR and is found to be weakly exogenous with respect to the long run coefficients in the model. This motivates why we focus on housing prices and credit in modeling the short run adjustments.

Second, the dynamic interaction between housing prices and credit is also analyzed using system methods. Full information maximum likelihood is used in the design of the short run specifications, which is carried out general to specific. Previous studies have resorted to an equation-by-equation approach at this stage.

Third, the paper includes a measure of households expectations about the future development in their own as well as the Norwegian economy in the dynamic specification. As a housing purchase is a long term investment, this seems to be a highly relevant variable to include in a housing price equation. Indeed, it is shown that this variable has a positive and significant impact on housing prices.

While many previous studies have had difficulties measuring supply side effects, our results indicate a large and negative supply elasticity in the long run. This suggests that supply side constraints are important for long run movements in prices and that a liberalization of zoning regulations and other regulations limiting the supply of housing might be an effective tool to prevent a rapid increase in housing prices.

Finally, dynamic simulations demonstrate how shocks are propagated and amplified across the two markets over time. When we take the analysis one step ahead and include a separate model for the supply side, the effects of a positive shock to housing prices or to credit are dampened over time as residential investments gradually shift the supply of housing.

The paper gives a survey of the recent literature in Section 2. A description of the Norwegian housing and credit markets is outlined in Section 3. Section 4 provides a brief theory discussion, while we investigate the fundamental determinants of housing prices and household debt in Section 5 by means of a multivariate cointegration analysis. Section 6 describes the dynamic interaction between the two variables. The model yields meaningful short and long term effects when estimated on the sample 1986q2-2008q4. In Section 7 we compare our basic model for housing prices and household debt with an enlarged version which also includes the supply of housing. In both cases dynamic simulations demonstrate that there are self-reinforcing feedback effects between the two variables of interest. Section 8 concludes.

2 A survey of empirical contributions

The empirical literature on housing prices is extensive; see *e.g.* Hendry (1984), Muellbauer and Murphy (1997), Pain and Westaway (1997), Meen (2001, 2002) and Malpezzi (1999) to mention a few important contributions. Girouard et al. (2006) provide a nice overview of the empirical literature. The majority of the papers have

investigated the determinants of housing prices within a single equation set-up. That framework does not shed light on the possible interaction between housing prices and household borrowing. Only recently – in the past decade – a literature on the nexus of housing prices and credit has emerged. The results up to now disagree about the direction of causality. The discrepancies can, however, be ascribed a number of sources: there are institutional differences between countries, and the methodological approaches as well as sample sizes and data sets vary across the studies. A summary of the empirical findings, which we refer to below, are given in Table 1 and Table 2.

Table 1: Findings in the literature: Long run interaction

Author(s)	Long run interaction		
	$ph \rightarrow d$	$ph \leftarrow d$	$ph \leftrightarrow d$
Hofmann (2003, 2004)	*		
Brissimis and Vlassopoulos (2009)	*		
Gerlach and Peng (2005)	*		
Oikarinen (2009a,b)		*	
Fitzpatrick and McQuinn (2007)			*
Berlinghieri (2010)			*
Gimeno and Martínez-Carrascal (2010)			*

Table 2: Findings in the literature: Short run interaction

Author(s)	Short run interaction		
	$\Delta ph \rightarrow \Delta d$	$\Delta ph \leftarrow \Delta d$	$\Delta ph \leftrightarrow \Delta d$
Hofmann (2003)			*
Brissimis and Vlassopoulos (2009)			*
Gerlach and Peng (2005)	*		
Oikarinen (2009a,b) ^a		*	
Fitzpatrick and McQuinn (2007)		*	
Berlinghieri (2010)			*

^a The results apply to the period after the Finnish credit markets were deregulated.

In an early study, using both panel data and time series techniques for 20 countries, Hofmann (2003) finds a cointegrating relationship between property prices, bank lending and GDP. The equation is interpreted as a credit equation and property prices are found to affect private sector borrowing in the long run, while the opposite direction of causation is not supported. The data are quarterly and cover the period 1985-2001. The author also reports results for the short run dynamics, where he finds causality to go in both directions. The long run results are further corroborated in Hofmann (2004)², where he first studies VARs in real credit to the private sector, GDP (as a broad measure of economic activity) and the short-term real interest rate as a measure of financing costs for each country. For a majority of the countries, the Johansen analysis (Johansen (1988)) shows no cointegration with this information set. When he extends the analysis to include real property

²See also Goodhart and Hofmann (2007).

prices in the VARs, Hofmann finds strong support for one cointegrating vector for all countries, which (through the significance of the loadings) can be interpreted as a credit equation for those countries where a high share of loans are secured by real estate.

This finding is supported by Brissimis and Vlassopoulos (2009) in a single country study for Greece. With quarterly data specific to the housing market for the period 1993-2005, they find only one cointegrating relationship based on multivariate cointegration techniques. This is interpreted as a mortgage loan equation, where loans are determined by housing prices, interest rates and an income measure. The loadings reveal that only the credit variable equilibrium corrects, i.e. housing prices are found to be weakly exogenous with respect to the long run parameters. Hence, in a long run perspective, the causation does not run from mortgage lending to housing prices. In the short run they find evidence of a contemporaneous bi-directional dependence.

Gerlach and Peng (2005) examine the interaction between credit to the private sector and residential property prices with a sample of quarterly data for Hong Kong from 1984 to 2001. They use a vector error correction framework and find that the direction of causation is from housing prices to private sector debt both in the long run and in the short run.

Contrary to this, Oikarinen (2009b) finds the direction of causation to go from household borrowing to housing prices in the long run. He uses quarterly data for Finland from 1975 to 2006 to explore the mutual dependence between housing prices and borrowing. A cointegration analysis in the spirit of Johansen (1988) supports the existence of only one cointegrating vector, which is interpreted as a housing price equation. Tests for Granger non-causality show that there is no dynamic effect going in either direction before 1988, *i.e.* before the Finish credit market was considered fully deregulated. There is however an effect on housing prices from the credit market running via the error correction term. After the deregulation, however, lending is shown to Granger cause housing prices also through the short run dynamics, while the opposite is not found to be the case. Furthermore, both variables are affected by the error correction term in the short run after deregulation. These results are corroborated by an impulse response analysis, where Oikarinen establish an interaction between housing prices and credit only after the deregulation process was considered completed (after 1987). Using the same methodological framework, Oikarinen (2009a) reports similar results with regional housing price data for the Helsinki Metropolitan area. Again, household debt enters the long run relationship for housing prices and Granger non-causality tests give the same results as in Oikarinen (2009b).

There are also a few recent studies documenting a mutual dependency in the long run, *i.e.* two cointegrating vectors are found. Fitzpatrick and McQuinn (2007) look at the interaction between housing prices and mortgage credit in Ireland between 1981 and 1999. They show that the two variables are mutually dependent in the long run, as well as in the short run. In the dynamic specification a contemporaneous effect is only established from credit to housing prices, while housing prices are found to have lagged effects on credit. Like Hofmann (2003), Fitzpatrick and McQuinn (2007) analyze the long run dependence within a single equation framework

adopting the original approach to cointegration of Engle and Granger (1987).³

When exploring the dynamic interaction between housing prices and credit, the two equations are estimated separately by OLS and a general to specific procedure is followed to find a parsimonious system. Acknowledging the potential endogeneity problems, Fitzpatrick and McQuinn estimate the two equations jointly by non linear three stage least squares after having sequentially reduced the dimensionality of the two equations.⁴

The results of Fitzpatrick and McQuinn (2007) are supported by Berlinghieri (2010) for quarterly US data covering the period 1977 to 2005 who also finds a bi-directional interdependence in the short run. A two step Engle-Granger approach is adopted and the short run dynamics are estimated by single equation OLS. The interaction is found to run in both directions also in the short term.

Making use of quarterly data for the period 1984-2009, Gimeno and Martínez-Carrascal (2010) study the interaction between housing prices and household borrowing in Spain. A multivariate cointegration analysis shows that the two variables are interdependent in the long run, *i.e.* that housing prices affect mortgage credit in the long run, and vice versa. Further, the loading factors imply that disequilibrium in the credit market leads to adjustments in both markets, while only housing prices error correct to disequilibrium constellations in the housing market. They do not report results for the short run dynamics.

The diverging results, as summarized in Table 1 and Table 2 call for further research. Our paper adopts the same econometric approach as Gimeno and Martínez-Carrascal (2010), but we go further. Not only do we to study the long run interaction, but also the dynamic interaction between the two markets, which is important for both policy evaluation and forecasts.

The studies that address the short run interaction by modeling the dynamics of the two variables all use a single equation approach, *i.e.* the equations are estimated separately by OLS regressions. In some cases the system is estimated jointly by 3SLS after the dimensionality of the equations in the system have been reduced separately or Hausman tests are run to test the consistency of the OLS estimates. This may be inappropriate – as pointed out by Hammersland and Jacobsen (2008) – because the single equation specifications will themselves be affected by the reduction process if we believe the variables in the system are jointly determined in the first place. From this perspective, it seems highly relevant to deal with the potential simultaneity from the onset. Hence, one should design the structural short run model using system methods that takes on the simultaneity problem from the outset.

3 The Norwegian housing and credit markets

The banking crisis in Norway that took place between 1988-1993 is a clear example of a collapse of property prices being followed by imbalances in the real economy. The

³Hofmann (2003) also considers a Johansen analysis, but it is the results from the single equation procedure that are retained for the dynamic specifications.

⁴In addition to an equation for housing prices and one for household debt, Fitzpatrick and McQuinn (2007) adds an additional equation for the supply side of the housing market to their system. This equation is taken from a former study (McQuinn, 2004) and hence it is not directly integrated in their analysis.

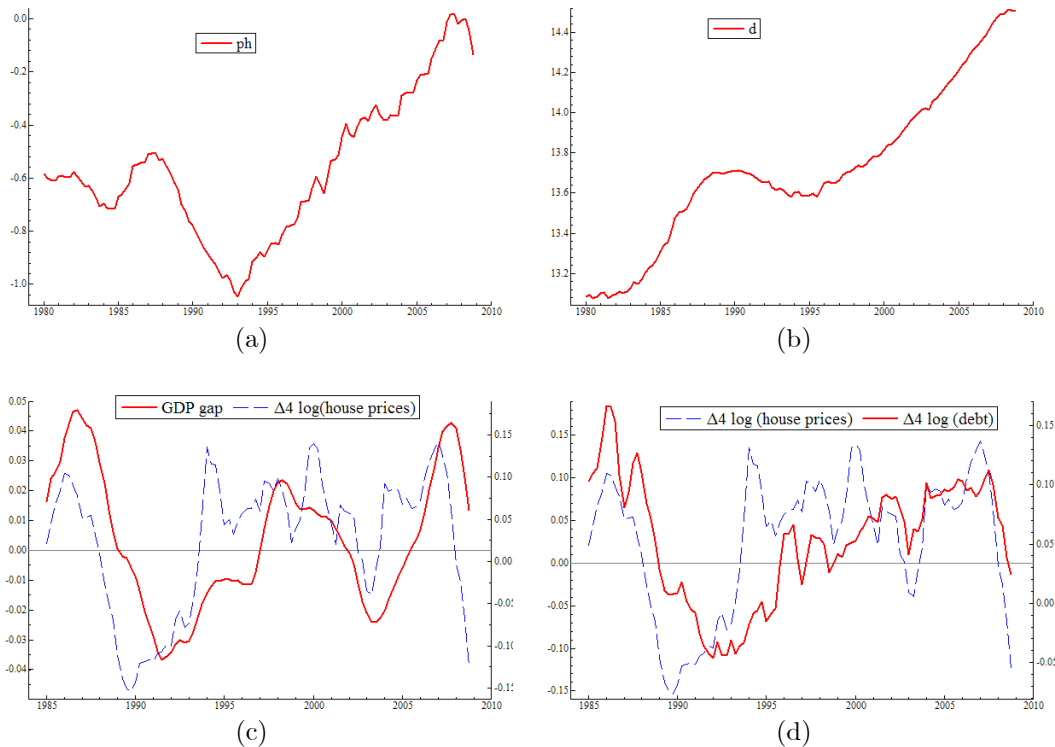


Figure 1: Panel a) Log of real housing prices, 1980-2008. Panel b) Log of real household debt, 1980-2008. Panel c) GDP gap (left scale) and four quarter growth in real housing prices (right scale), 1985-2008. Panel d) Four quarter growth in real housing prices (left scale) and in real household debt (right scale), 1985-2008.

recent financial crisis was different in that it was an external shock to the domestic economy, which had a significant, but short-lived, negative effect on Norwegian housing prices.

Krogh (2010) gives a detailed account of the changes in the Norwegian credit market regulations and other major events in the period 1970-2008. This time span entails a period with strict credit market regulations in the 1970s, a gradual deregulation of these markets in the 1980s, followed by the banking crisis, and the subsequent development up to the advent of the current financial crisis.

For our purpose it is important to note that also the housing market was deregulated in 1982, shortly before the credit market regulations were lifted. The combined effect of these liberalization processes was a boom in the real estate market, made possible and financed by a credit expansion. The problems facing the banking sector when the bubble burst became immense (Vale, 2004). After the Norwegian banking crisis, which ended in 1993, real housing prices have grown almost consecutively until the financial meltdown of the previous decade (see Figure 1a). Growing housing prices have been accompanied by a substantial expansion in real household debt (see Figure 1b).

The historical episodes referred to above strongly suggest there is an interdependency between the evolution of real housing prices and that of real household debt. For an impression of how housing price developments relate to the general macroeconomic picture in Norway, Figure 1c plots the four quarter growth in real

housing prices against percentage deviations of GDP mainland Norway from trend.⁵ A close link between economic activity and housing prices is apparent over the entire period, with a less pronounced correlation pattern the last few years. Goodhart and Hofmann (2007) argue that there will be a tendency of changes in housing price growth to lead *peaks* and *troughs* in economic activity. This may suggest that turning points in the housing market are indicators of future economic developments. Figure 1c shows such a tendency for the case of Norway in the period after deregulation. Housing prices may affect economic activity through wealth effects on private consumption and a rise in house prices also raise the value of housing relative to construction costs, that is the Tobin q (Tobin, 1969) for residential investments. Another channel in which housing prices could have an effect on the business cycle is by amplifying shocks in the credit market. It is evident from Figure 1d, where we have plotted the four quarter growth in real housing prices against four quarter growth in real household borrowing, that the two series seem to move quite closely together.

Previous studies of the credit and housing markets in Norway do not take the potential simultaneity between the two into account. For example, the determination of household debt is the topic of Jacobsen and Naug (2004), whilst Jacobsen and Naug (2005) describe a separate model for housing prices. In Jacobsen and Naug (2004), housing prices are one of the fundamental factors explaining household debt, whereas household borrowing is not part of the cointegrated vector explaining housing prices in Jacobsen and Naug (2005)⁶. That said, it is documented that the interest rate is an important determinant of housing prices. Also, Jacobsen and Naug (2004) find that the interest rate is one of the fundamental factors explaining household borrowing. The effect of interest rates on credit thus suggests that the interest rate variable in the housing price equations captures a credit effect, *i.e.* that the coefficient of the interest rate in Jacobsen and Naug (2005) picks up a gross effect.⁷

4 Economic theory

The commonly used framework for modeling housing price is the life-cycle model, see *e.g.* Meen (2001, 2002), Muellbauer and Murphy (1997, 2008) and the references therein. We augment this model with a term capturing the presence of credit constraints, and the marginal rate of substitution (MRS) between housing and a composite consumption good is then given by (see *e.g.* Meen (1990) or Meen and Andrew (1998)):

⁵GDP mainland Norway measures total production in Norway excluding extraction of oil and gas as well as other production related to this.

⁶Jacobsen and Naug (2005) tested for the significance of a credit variable in their specification, but found no significant effects.

⁷Akram et al. (2006), Akram et al. (2007) and Andersen (2011) augment the core part of a macroeconomic model for the Norwegian economy (see *e.g.* Bårdsen et al. (2003) and Bårdsen et al. (2005)) with different versions of the housing price and credit equations of Jacobsen and Naug (2004, 2005). These studies address issues related to financial stability when there are interaction effects between housing prices and credit.

$$(1) \quad MRS = PH_t[(1 - \tau)i_t - \pi + \delta - (dph_t^e/dt)/ph_t + \lambda_t/\mu_c],$$

where PH_t is real housing prices, τ is the marginal tax rate on equity income, i_t is the nominal interest rate (paid by households for loans), π is the annual inflation rate, δ is the depreciation rate or the rate of maintenance costs including property taxation, and $(dph_t^e/dt)/ph_t$ is the expected rate of appreciation for housing prices. λ_t is the shadow price of the credit constraint which is divided by the marginal utility of consumption μ_c . This is commonly known as the real housing user cost of capital, in this case augmented with a credit constraint. Market efficiency requires that the following arbitrage relationship holds, where Q_t represents the real imputed rental price for housing services

$$(2) \quad PH_t = Q_t/[(1 - \tau)i_t - \pi + \delta - (dph_t^e/dt)/ph_t + \lambda_t/\mu_c]$$

Meen (2002) follows Poterba (1984) and interprets (2) as an inverted housing stock demand function. If we assume that Q_t , which is unobservable, is a function of real disposable income for the household sector (excluding dividends), YH_t , and the stock of dwellings, H_t , we can write the inverted demand function as

$$(3) \quad PH_t = f^*(H_t, YH_t, R_t, (dph_t^e/dt)/ph_t, \lambda_t/\mu_c),$$

where R_t is the real after tax interest rate $(1 - \tau)i_t - \pi$.

We will assume that price expectations influence housing prices only in the short run. Furthermore, we shall substitute household loans as a proxy for the theoretically correct – but unobservable – λ_t/μ_c term in (3). Our empirical study can thus be seen as a test of the informational value of household loans when direct information on credit constraints is missing. As household debt is non-stationary, we implicitly assume that the same holds for the shadow price of the credit constraint.

Hence, we formulate the determination of real housing prices at the aggregate level in a static long run equilibrium as

$$(4) \quad PH_t = f(H_t, YH_t, R_t, D_t),$$

where $\frac{\partial f}{\partial H} < 0$, $\frac{\partial f}{\partial YH} > 0$, $\frac{\partial f}{\partial R} \geq 0$, $\frac{\partial f}{\partial D} > 0$ and D_t is real household debt.

Equation (4) expresses market clearing prices for any given housing stock. The equation describes housing prices as an increasing function of disposable income and household debt, while a greater supply of housing services is expected to push housing prices down. The sign of the derivative with respect to the interest rate is ambiguous. The main effects of a change in the interest rate work through disposable income and household loans, which both are controlled for in (4). What remains are the substitution effects which may be of either sign from a theoretical point of view.⁸

⁸It is not only from a theoretical point of view that the sign of the direct effect is ambiguous. Empirically it is often found to be statistically insignificant. In the case of Norway the dominant interest rate effects on housing prices are indirect. Almost all mortgage debt in Norway are loans with flexible interest rates. Hence, a change in interest rates will immediately feed into the disposable income for households, and it is likely to pick up the main effect of interest rates on demand for housing. The inclusion of the credit aggregate captures the effect on housing prices from a change in the cost of financing.

We supplement our model for housing prices with a relationship that determines real household debt in a long run equilibrium,

$$(5) \quad D_t = g(H_t, YH_t, R_t, PH_t, TH_t),$$

where $\frac{\partial g}{\partial H} > 0$, $\frac{\partial g}{\partial YH} > 0$, $\frac{\partial g}{\partial R} < 0$, $\frac{\partial g}{\partial PH} > 0$, $\frac{\partial g}{\partial TH} > 0$ and TH_t denotes housing turnover. Equation (5) is an extended version of Fitzpatrick and McQuinn (2007). It defines household debt as a function of the housing stock, housing prices, the interest rate, disposable income and the housing turnover. In our specification, the housing stock and the housing turnover are additional explanatory variables.

In the following we shall think of equations (4) and (5) as a subsystem, conditioning on H_t, YH_t, R_t , and TH_t . The last three variables can be assumed to be determined by factors other than housing prices and credit. The housing stock, H_t , on the other hand represents the supply side of the housing market. It appears in equation (3) since it affects negatively the market clearing rent and hence the price of housing. We will assume it is related to the profitability of new construction and thus that it is influenced positively by real housing prices and negatively by construction costs. Hence, there are feedback effects from housing prices via H_t to housing prices and credit. In order to capture these feedback effects we estimate a submodel for housing supply separately in Appendix A. In Section 7, when we compare the dynamic responses from our baseline model with those from an extended version of the model which includes the housing supply, we find that the effects of a shock to housing prices or household debt are dampened.

5 Cointegration analysis

In order to construct a joint model for housing prices and household loans we first estimate their long run determinants in a cointegrated VAR system where also the household income is treated as an endogenous variable. Finding cointegration ensures that we can formulate a vector error correction model (VECM).

The VECM approach provides an opportunity to study long run determinants and short run dynamics in a unified framework, which is open for the possibility that the causality between housing prices and credit is bi-directional. The model is therefore suitable for addressing the key issue: Is there empirical evidence for the existence of a financial accelerator in the Norwegian housing market?

A semi-logarithmic transformation of the variables appearing in equations (4) and (5) – which can be seen as a linearization of the theoretical formulations – forms the basis for the information set underlying our empirical analysis. All data are seasonally unadjusted and in what follows, small letters indicate that the variables are measured on a logarithmic scale.⁹ All monetary variables are measured in real terms, having been deflated by the consumption deflator. Our sample covers the period 1986q2-2008q4. We have data for the number of house transactions only from 1985q1 and the data for housing prices are also less reliable in the period prior to this. The deregulation of the housing and credit markets in the early 1980's is likely

⁹For a detailed data description, see Appendix A. The log transformation is applied to all variables in (4) and (5), except the real after tax interest rate.

to have altered the functioning of both, so that a different model would probably be more appropriate if we were to consider the period prior to the deregulation.

In the cointegration analysis, we start by estimating a fifth order VAR in real housing prices, real household debt and real disposable income, conditioning on the real after tax interest rate, the housing turnover and the housing stock. The VAR(5) may be reparameterized in the following way:

$$(6) \quad \Delta \mathbf{x}_t = \mathbf{\Pi} \mathbf{y}_{t-1} + \sum_{i=1}^4 \mathbf{\Gamma}_i \Delta \mathbf{x}_{t-i} + \sum_{i=0}^4 \mathbf{\Psi}_i \Delta \mathbf{z}_{t-i} + \mathbf{\Phi} \mathbf{G}_t + \boldsymbol{\epsilon}_t,$$

where $\boldsymbol{\epsilon}_t \sim N(0, \boldsymbol{\Sigma})$, \mathbf{x}_t is a 3×1 vector comprising the endogenous variables ph,d and yh. $\mathbf{y} = (\mathbf{x}', \mathbf{z}')$ is a $(3+3) \times 1$ vector where \mathbf{z} is a 3×1 vector composed of the exogenous variables R, th and h. \mathbf{G}_t is a vector of deterministic terms (constant, linear trend and centered seasonal dummies), and $\mathbf{\Pi}$, $\mathbf{\Gamma}_i$, and $\mathbf{\Psi}_i$ and $\mathbf{\Phi}$ are the corresponding coefficient matrices.

The linear trend is restricted to enter the cointegration space. This implies that equation (6) can be written as:

$$(7) \quad \Delta \mathbf{x}_t = \tilde{\mathbf{\Pi}} \tilde{\mathbf{y}}_{t-1} + \sum_{i=1}^4 \mathbf{\Gamma}_i \Delta \mathbf{x}_{t-i} + \sum_{i=0}^4 \mathbf{\Psi}_i \Delta \mathbf{z}_{t-i} + \tilde{\mathbf{\Phi}} \tilde{\mathbf{G}}_t + \boldsymbol{\epsilon}_t$$

where $\tilde{\mathbf{\Pi}} = (\mathbf{\Pi}, \boldsymbol{\delta})$ and $\tilde{\mathbf{y}} = (\mathbf{y}', t)'$ with $\boldsymbol{\delta}$ representing the vector of trend coefficients. Further, $\tilde{\mathbf{G}}_t$ comprises only a constant and centered seasonal dummies with the corresponding coefficient matrix being given as $\tilde{\mathbf{\Phi}}$.

The orders of integration of the data series have been examined by a suite of different tests; the Augmented Dickey-Fuller (ADF) test (Dickey and Fuller (1979)), the Phillips-Perron (PP) test (Phillips (1987) and Phillips and Perron (1988)), as well as the Kwiatkowski, Phillips, Schmidt, and Shin (KPSS) test (Kwiatkowski et al. (1992)), see Table D.1 in Appendix D. While the ADF test and the PP test have non-stationarity as the null, the KPSS test has stationarity as the null, which is important to keep in mind when inspecting the test results displayed in Table D.1 of Appendix D. We test for the possibility of both I(0) (levels are stationary) and I(1) (first differences are stationary), and, if those tests are inconclusive, we also test for the possibility of the variable being I(2) (the second difference is stationary).

As a guidance for choosing the optimal lag truncation for the ADF tests, we have relied on Akaike's information criterion (AIC) starting with an initial lag length of eight in the first differences in all test regressions and then choose the specification with the lowest AIC value.

Judging from the three tests for integration, it appears that the majority of the time series in our sample can be treated as integrated of order one for modeling purposes. The real after tax interest rate appears to be stationary according to all the tests, which does not impose any problems for the empirical analysis. The main concern when applying standard cointegration techniques is the presence of I(2) variables. Though including I(2) variables does not affect the consistency of the estimated coefficients in the CVAR model (they are in fact super-super consistent), it might modify the interpretation of the results (see *e.g.* Juselius (2006)).

Table 3: Trace test for cointegration ^a

<i>Eigenvalue</i> : λ_i	H_0	H_A	λ_{trace}	5%-critical value ^b
0.39	$r = 0$	$r \geq 1$	86.59	64.48
0.22	$r \leq 1$	$r \geq 2$	41.74	40.95
0.19	$r \leq 2$	$r \geq 3$	18.82	20.89
Diagnostics ^c	Test statistic	Value[p-value]		
Vector AR 1-5 test:	F(45,146)	1.06 [0.39]		
Vector Normality test:	$\chi^2(6)$	7.78 [0.26]		
Vector Hetero test:	F(270,247)	1.03 [0.42]		
Estimation period:	1986q2-2008q4			

^a Endogenous variables: Real housing prices, real household debt and real disposable income. Restricted variables: Real interest rate after tax, housing turnover, housing stock and a trend. Unrestricted variables: Constant and centered seasonal dummies for the first three quarters.

^b Critical values are obtained from Table 13 in Doornik (2003) - with 3 exogenous variables.

^c See Doornik and Hendry (2009b).

While the ADF test indicates that housing prices and household debt are $I(2)$ ¹⁰, it is inconclusive with respect to the housing stock. According to PP and KPSS, however, both housing prices and household debt are found to be $I(1)$. The housing stock is however found to be $I(2)$ in one case (PP) and $I(1)$ in the other (KPSS).

As the results regarding the order of integration diverge among the tests, we shall treat all variables as integrated of order one at most in the econometric analysis, keeping these caveats in mind.

According to AIC, the VAR-model should include 5 lags in the endogenous variables (tests are not reported here). To determine the lag length of the exogenous variables included in the information set, we report a series of Wald F-tests (see the lower part of Table D.3 in Appendix D). Judged by these tests it is sufficient to include only one lag in each of the exogenous variables. The same lag structure is implied if we instead rely on AIC.

The trace test for the order of cointegration (Johansen, 1988) can be used to determine the rank of the matrix $\tilde{\Pi}$, which corresponds to the number of independent linear combinations between the variables that are stationary. Table 3 displays the results. When correcting for the inclusion of exogenous variables (see Doornik (2003)), the test indicates that there are two cointegrating vectors. The model is well specified – residual diagnostics show that the residuals are neither heteroskedastic nor autocorrelated, and normality is not rejected.

We follow Johansen (1988) and define $\tilde{\Pi} = \alpha\beta'$, where β is a $(p + q + 1) \times r$ matrix and α is a $p \times r$ matrix corresponding to the long run coefficients and loading factors respectively. The rank of the $\tilde{\Pi}$ matrix is denoted by r , while p refers to number of endogenous variables and $q + 1$ is the number of exogenous variables (including the deterministic trend, which is restricted to lie in the cointegration space). Given that the rank of $\tilde{\Pi}$ is two, with three endogenous and three exogenous variables, the cointegrating part of equation (6) takes on the following form:

¹⁰Actually the test is inconclusive for the credit variable as it rejects non-stationarity of the levels as well as for the second difference, while non-stationarity is not rejected for the first difference.

(8)

$$\alpha\beta'y = \begin{pmatrix} \alpha_{1,ph} & \alpha_{1,d} \\ \alpha_{2,ph} & \alpha_{2,d} \\ \alpha_{3,ph} & \alpha_{3,d} \end{pmatrix} \begin{pmatrix} \beta_{ph,1} & \beta_{d,1} & \beta_{yh,1} & \beta_{R,1} & \beta_{th,1} & \beta_{h,1} & \beta_{t,1} \\ \beta_{ph,2} & \beta_{d,2} & \beta_{yh,2} & \beta_{R,2} & \beta_{th,2} & \beta_{h,2} & \beta_{t,2} \end{pmatrix} \begin{pmatrix} ph \\ d \\ yh \\ R \\ th \\ h \\ t \end{pmatrix}$$

Exact identification can be achieved by imposing two restrictions in each vector. We start by normalizing on real housing prices in the first vector ($\beta_{ph,1} = 1$) and real household debt in the other ($\beta_{d,2} = 1$). In addition, it is assumed that the housing turnover has no direct effect on real housing prices ($\beta_{th,1} = 0$). This is in accordance with the theoretical housing price equation (4), while earlier studies have found that the turnover affects household borrowing in Norway (see Jacobsen and Naug (2004)), which suggests that it should be part of the relationship determining household debt. The final restriction we use for exact identification is that it is the value of the housing capital – and not simply housing prices – which determines the size of the collateral. To incorporate this into the empirical framework, we assume that a change in either the housing stock or housing prices have the same effect on household debt ($\beta_{ph,2} = \beta_{h,2}$).

Based on the identified cointegrated vectors, we can move on to test overidentifying restrictions. The results of these restrictions are documented in Table 4 and Table 5 below.¹¹ For every new restriction that is imposed, we report both the log-likelihood value, the incremental test as well as the total test at the bottom line of each panel. In Panel 1 the trend variable is dropped from both equations ($\beta_{t,1} = \beta_{t,2} = 0$), which correspond to two testable overidentifying restrictions. Next, in Panel 2, we omit the real after tax interest variable from the vector associated with the real housing price ($\beta_{R,1} = 0$). As mentioned above, this does not imply that a change in the interest rate will not affect housing prices, but it means that interest rate effects are captured by changes in disposable income and through the credit channel.¹² In Panel 3 there is no effect of disequilibrium in the housing market on household debt ($\alpha_{2,ph} = 0$), whereas Panel 4 shows the case with no direct effect of real disposable income on household debt ($\beta_{yh,2} = 0$). Finally, Panel 5 shows the result when we impose that the loadings of both cointegrating vectors with respect to income are zero ($\alpha_{3,ph} = \alpha_{3,d} = 0$), *i.e.* the test shows weak exogeneity of income with respect to the long run coefficients, see Johansen (1992). According to the incremental tests reported in Table 4, all individual restrictions are supported by the data and the p-value for the joint test of all restrictions is 0.3.

The coefficients reported in Panel 5 in Table 2 describe the two final long run relationships for housing prices and household debt. The loadings for the error correction terms at all steps in the reduction process are reported in Table 3. Our

¹¹The absolute value of standard errors are reported in parantheses below the estimated coefficients.

¹²Gimeno and Martínez-Carrascal (2010) and Fitzpatrick and McQuinn (2007) are excluding the real interest rate from the long run equation for housing prices by assumption.

Table 4: Testing steady-state hypotheses.

<p>The just identified house price and debt equations are defined by</p> $\beta_{ph,1} = 1, \beta_{d,2} = 1, \beta_{th,1} = 0, \beta_{ph,2} = \beta_{h,2} \text{ in (8)}$ $\text{Log}L = 844.751$	
<p>Panel 1: Testing no trend ($\beta_{t,1} = \beta_{t,2} = 0$)</p> $ph = \underset{(0.07)}{0.76}d + \underset{(0.21)}{1.39}yh - \underset{(0.37)}{2.00}h + \underset{(0.85)}{0.13}R$ $d = \underset{(0.17)}{1.53}ph - \underset{(1.40)}{1.45}yh - \underset{(1.40)}{0.71}R + \underset{(0.05)}{0.09}th + \underset{(0.07)}{1.53}h$ $\text{Log}L = 842.845, \quad \chi^2(2) = 3.81[0.15]$	
<p>Panel 2: No effect of real after tax interest rate on house prices ($\beta_{R,1} = 0$)</p> $ph = \underset{(0.08)}{0.77}d + \underset{(0.22)}{1.43}yh - \underset{(0.40)}{2.07}h$ $d = \underset{(0.18)}{1.54}ph - \underset{(0.40)}{1.48}yh - \underset{(0.40)}{0.54}R + \underset{(0.05)}{0.10}th + \underset{(0.07)}{1.54}h$ $\text{Log}L = 842.834, \quad \chi^2(1) = 0.02[0.88], \quad \chi^2(3) = 3.84[0.28]$	
<p>Panel 3: No effect of disequilibrium housing prices on household debt ($\alpha_{2,ph} = 0$)</p> $ph = \underset{(0.19)}{0.84}d + \underset{(0.65)}{1.67}yh - \underset{(1.18)}{2.58}h$ $d = \underset{(0.85)}{1.08}ph - \underset{(2.35)}{1.18}yh - \underset{(2.35)}{3.98}R + \underset{(0.28)}{0.56}th + \underset{(0.30)}{1.08}h$ $\text{Log}L = 842.276, \quad \chi^2(1) = 1.12[0.29], \quad \chi^2(4) = 4.95[0.29]$	
<p>Panel 4: No effect of real disposable income on household debt ($\beta_{yh,2} = 0$)</p> $ph = \underset{(0.19)}{0.86}d + \underset{(0.64)}{1.42}yh - \underset{(1.16)}{2.33}h$ $d = \underset{(1.87)}{0.78}ph - \underset{(1.87)}{2.83}R + \underset{(0.15)}{0.24}th + \underset{(0.15)}{0.78}h$ $\text{Log}L = 841.323, \quad \chi^2(1) = 1.12[0.29], \quad \chi^2(5) = 6.86[0.23]$	
<p>Panel 5: Imposing weak exogeneity of income with respect to the long run coefficients ($\alpha_{3,ph} = \alpha_{3,d} = 0$):</p> $ph = \underset{(0.19)}{0.98}d + \underset{(0.63)}{1.69}yh - \underset{(1.15)}{3.03}h$ $d = \underset{(1.79)}{0.76}ph - \underset{(1.79)}{2.74}R + \underset{(0.15)}{0.28}th + \underset{(0.16)}{0.76}h$ $\text{Log}L = 840.529, \quad \chi^2(2) = 1.59[0.451], \quad \chi^2(7) = 8.44[0.30]$	
<p>The sample is 1986q2 to 2008q4, 91 observations.</p>	

results support the hypothesis that housing prices and household borrowing are mutually dependent in the long run. All long run coefficients have the expected signs in the final model (Panel 5) and they are significant at conventional significance levels.¹³

The semi-elasticity of household borrowing with respect to the real interest rate after tax is -2.74 , implying that a one percentage point increase in the real interest rate will decrease household borrowing by almost three percent in the long run. This is lower (in absolute value) than the estimate found for Spain by Gimeno and Martínez-Carrascal (2010) who consider nominal instead of real interest rates. It is however greater than the estimates found by Brissimis and Vlassopoulos (2009) for Greece and Fitzpatrick and McQuinn (2007) for Ireland who both consider real

¹³The interest rate is the only exception. However, using a one sided test, which appears to be meaningful, it is found to be significant at the 10 % level (p-value = 0.068). The fact that it is also highly significant from an economic point of view suggests that it should not be excluded.

Table 5: Loading factors.

Loading	Panel 1	Panel 2	Panel 3	Panel 4	Panel 5
$\alpha_{1,ph}$	-0.82 0.21	-0.76 0.20	-0.21 0.04	-0.22 0.04	-0.24 0.04
$\alpha_{1,d}$	-0.44 0.14	-0.40 0.13	-0.06 0.02	-0.08 0.03	-0.1 0.03
$\alpha_{2,ph}$	-0.13 0.11	-0.13 0.11	0 --	0 --	0 --
$\alpha_{2,d}$	-0.11 0.07	-0.10 0.07	-0.04 0.01	-0.05 0.01	-0.04 0.01
$\alpha_{3,ph}$	0.42 0.15	0.40 0.14	-0.04 0.03	-0.05 0.03	0 --
$\alpha_{3,d}$	0.31 0.1	0.29 0.09	0.002 0.02	-0.01 0.02	0 --

interest rates. Even though there is no direct causal link between real housing prices and the real interest rate in our model, a higher interest rate implies that housing prices will fall as it reduces the demand for housing by altering the credit variable, which is found to be highly significant in the housing price equation.

The estimated elasticity of housing prices with respect to household debt is 0.98. This is lower than the elasticity reported by Fitzpatrick and McQuinn (2007), but higher than the estimate in Gimeno and Martínez-Carrascal (2010). We find that the credit aggregate exercises a greater impact on housing prices than do housing prices on credit in a long run perspective, a result that parallels the finding of Fitzpatrick and McQuinn (2007). A one percent increase in housing prices will increase household borrowing by 0.76 *percent* in the long run.

The loadings imply that both housing prices and household debt error correct when the latter departs from the value implied by its fundamentals. Moreover, the analysis indicates that only housing prices error correct when deviating from its steady state level. This result is supported by Gimeno and Martínez-Carrascal (2010).

6 Short run dynamics

This section addresses the short run dynamics by estimating a structural vector error correction model (SVECM). We obtain the representation of the simultaneous equation system by premultiplying the reduced form representation in equation (7) by the contemporaneous feedback matrix, \mathbf{B} :

$$(9) \quad \mathbf{B}\Delta\mathbf{x}_t = \mathbf{B}\tilde{\Pi}\tilde{\mathbf{y}}_{t-1} + \sum_{i=1}^4 \mathbf{B}\Gamma_i\Delta\mathbf{x}_{t-i} + \sum_{i=0}^4 \mathbf{B}\Psi_i\Delta\mathbf{z}_{t-i} + \mathbf{B}\epsilon_t$$

where we now define $\mathbf{B}\tilde{\Pi} = \mathbf{B}\alpha\beta' = \alpha^*\beta'$, $\mathbf{B}\Gamma_i = \Gamma_i^*$, $\mathbf{B}\Psi_i = \Psi_i^*$, $\mathbf{B}\epsilon_t = \epsilon_t$. In the interest of simplicity, we have left out the deterministic terms, $\tilde{\mathbf{G}}_t$, from the equation. The new error term will also be IIN with zero mean and variance-covariance matrix given by: $\mathbf{\Omega} = E(\epsilon_t\epsilon_t') = \mathbf{B}E(\epsilon_t\epsilon_t')\mathbf{B}' = \mathbf{B}\Sigma\mathbf{B}'$.

As the income variable is found to be weakly exogenous, we can write the above system as a conditional system for housing prices and credit and a marginal model

for income (see e.g. Johansen (1992)). Since the focus of this paper is the interaction between housing prices and credit, we can, without loss of generality, abstract from modeling the marginal model for income. In that case, the conditional SVECM takes the following form:

$$(10) \quad \Delta ph_t - b_{12}\Delta d_t = \sum_{i=1}^4 \Gamma_{1i}^* \Delta \mathbf{x}_{t-i}^* + \sum_{i=0}^4 \Psi_{1i}^* \Delta \mathbf{z}_{t-i}^* + \sum_{i=1}^4 \tilde{\Psi}_{1,Ri} \Delta R_{t-i} \\ + \alpha_{1,ph}^* ECM_{t-1}^{ph} + \alpha_{1,d}^* ECM_{t-1}^d + \varepsilon_{ph,t}$$

$$(11) \quad -b_{21}\Delta ph_t + \Delta d_t = \sum_{i=1}^4 \Gamma_{2i}^* \Delta \mathbf{x}_{t-i}^* + \sum_{i=0}^4 \Psi_{2i}^* \Delta \mathbf{z}_{t-i}^* + \sum_{i=1}^4 \tilde{\Psi}_{2,Ri} \Delta R_{t-i} \\ + \alpha_{2,ph}^* ECM_{t-1}^{ph} + \alpha_{2,d}^* ECM_{t-1}^d + \varepsilon_{d,t}$$

where we have normalized such that the contemporaneous feedback matrix, \mathbf{B} , has ones along the main diagonal. \mathbf{x}^* now consists of the two remaining endogenous variables, while \mathbf{z}^* still represents a vector of the current and lagged exogenous variables in the system (including the income variable) as well as a constant and seasonal dummies. Γ_{ji}^* , Ψ_{ji}^* and $\tilde{\Psi}_{j,Ri}$ ($j=1, 2$) are the short run coefficients, where $\Gamma_i^* = (\Gamma_{1i}^*, \Gamma_{2i}^*)$ and $\Psi_i^* = (\Psi_{1i}^*, \Psi_{2i}^*)$. Since the housing stock adjusts slowly, it is assumed to be fixed in the short run and is not part of the vector \mathbf{z}^* . Note also that we have excluded the contemporaneous value of the change in real after-tax interest rate, ΔR_t , from both equations to form our general unrestricted model. However, we supplement the short run dynamics by including an expectations variable, E , which measures households expectations about future developments in their personal economy and the macroeconomy. This variable can also be considered as a proxy for the expected rate of appreciation in housing prices, cf. Section 4. Hence, $\mathbf{z}^* = (th, E, yh)$. The expectations variable is only available from 1992q3 and is set to 0 in the period prior to this. The expectations variable has previously been adopted by Jacobsen and Naug (2005). They find a positive and significant short run effect of expectations on housing prices in a single equation framework.

As the equation system represented by equations (10) and (11) will be estimated and designed simultaneously, we once again have to face the tough and non trivial decision of how to exactly identify the system. To achieve exact identification, we have chosen to exclude the contemporaneous effect of the turnover in the housing price equation, while the credit equation is identified by omitting the contemporaneous value of the expectations variable. The just identified system is estimated by FIML (full information maximum likelihood). The resulting model produces well behaved residuals and serves as a starting point for the reduction process to obtain a parsimonious representation of the system.

A parsimonious model is found by stepwise elimination of insignificant variables in the system, which are excluded either one by one or in blocks. Unlike the single equation case, no algorithm for automatic general to specific search exists as yet, so we have carried out the search manually.¹⁴ In that process, we make sure

¹⁴See Doornik (2009) for a description of the automatic specification search in the case of a single equation.

that, according to the diagnostic tests, the Gaussian properties of the residuals are retained and that all imposed restrictions are supported by the data. In the preferred (final) model, we have chosen to retain some variables, which are relevant from *a priori* theoretical considerations, although they should have been excluded at the early stages of the reduction process had we followed a strict general to specific procedure. By doing so, we have achieved a more theoretically and intuitively appealing model formulation than we would have obtained otherwise, i.e if we had systematically eliminated the most insignificant variable at each stage. This procedure of structural model design results in the specifications displayed in Table 6.

Table 6: Short run dynamics ^a

Variable	Real housing prices		Real household debt	
	Coefficient	t-value	Coefficient	t-value
Constant	1.542	7.71	0.048	6.39
Δd_t	0.859	2.25	-	-
Δd_{t-1}	-	-	0.173	1.88
Δd_{t-3}	0.309	2.32	-	-
Δph_{t-4}	0.389	4.88	-	-
Δyh_{t-3}	-	-	0.197	3.31
ΔE_t	0.093	4.40	-	-
ΔE_{t-1}	0.098	4.41	-	-
ΔE_{t-2}	0.055	2.40	-	-
ΔR_{t-4}	-	-	-0.258	2.16
ECM_{t-1}^{ph}	-0.175	7.82	-	-
ECM_{t-1}^d	-0.059	2.23	-0.046	6.11
Dummy, q1	0.022	3.75	-0.004	1.18
Dummy, q2	0.021	3.65	-0.00001	0.02
Dummy, q3	0.012	2.05	-0.007	2.05
Sargan	$\chi^2(46) =$	55.79 [0.1528]		
Log likelihood	560.26			
σ	0.0143		0.0098	
Diagnosics ^b	Test statistic	Value [p-value]		
Vector EGE-AR 1-5 test:	F(20,140)	0.90 [0.59]		
Vector Normality test:	$\chi^2(4)$	5.34 [0.25]		
Vector hetero test:	F(183,81)	0.88 [0.76]		
Estimation Method	FIML			
Sample	1986q2-2008q4 ($T = 91$)			

^a Absolute t-values are reported.

^b See Doornik and Hendry (2009b).

Table 6 reveals that credit effects are important for housing price fluctuations also in the short run. We do not find any direct short run effect running from household debt to housing prices though. It is however clear that the credit aggregate will be influenced by housing prices through the error correction term present in the credit equation. Consistent with the cointegration analysis, the short run analysis indicates that both housing prices and household debt error correct when household

debt is high relative to its stable long run equilibrium and that only housing prices error correct when departing from their fundamentals. Our results suggest that if housing prices depart from their long run equilibrium by one percent, housing prices will fall by -0.175 percent. This is greater than what is found by Jacobsen and Naug (2005)¹⁵, but lower than the estimate reported by Fitzpatrick and McQuinn (2007).

Like Jacobsen and Naug (2004, 2005) and Fitzpatrick and McQuinn (2007), we find that the credit aggregate has a slower adjustment towards equilibrium when it is departing from its fundamentals than do housing prices. This is not a very surprising finding in light of the fact that the volume of debt is not easily changed over night. Gimeno and Martínez-Carrascal (2010), however, find the opposite to be the case for Spain.

All estimated coefficients have the expected signs. Interestingly, we find that changes in expectations have a great impact on housing prices. The full effect is reached after three quarters, *i.e.*, when there has been a change of ‘mood’. As anticipated, our estimation results show that the interest rate has a negative impact on household borrowing (and therefore indirectly on housing prices) and the income variable lagged three quarters enters the credit equation significantly with an expected positive sign. As the error correction term for household debt is present in the housing price equation, the interest rate feeds into housing prices also here. The diagnostics indicate that the model is well specified and we find support for the imposed restrictions (p-value = 0.1528). The residuals from the two estimated equations are clearly stationary (see Table D.2 in Appendix D).

Unlike previous studies (cf. Fitzpatrick and McQuinn (2007) and Brissimis and Vlassopoulos (2009)), the top-down approach applied in this paper consists of modeling the system simultaneously at all steps in the reduction process. Another approach, commonly used in the literature, is instead to simplify the two equations individually before estimating them as a system. Results from such an approach are reported in Tables C.1, C.2, and C.3 in Appendix C, where we have used the Autometrics package in PcGive (Doornik (2009)) to specify the individual equations before estimating them jointly by FIML. Again, the GUM is as defined by equations (10) and (11), and we restrict a constant and seasonal dummies to enter the model.

If we compare the results from the single equation specifications to the results obtained when the two equations, after each have been specified separately, are estimated jointly (*i.e.* the results in Table C.1 and C.2 compared to those in Table C.3) it is seen that the estimated coefficients change dramatically. It should be noted that the single equation approach does not pay heed to the issue of identification.

The model obtained from the equation-by-equation approach (Table C.3) and our preferred model from the structural model design (Table 6) are not nested, but we can make an informal comparison. The results reported in Table 6 are both more reasonable and easier to interpret from an economic point of view than those in Table C.3. Hence, it seems like our approach have some advantages compared to the traditional approach followed in the literature, see Appendix C for more details and discussion.

¹⁵Jacobsen and Naug (2005) only consider housing prices and not the interaction between housing prices and household debt.

7 Dynamic effects of shocks

In the previous section, we used a general to specific approach to specify a parsimonious system capturing the dynamic interaction between housing prices and credit. In the following we will use Monte Carlo simulations of this model to show the dynamic responses to exogenous shocks to the system. As a first step, we consider the subsystem of housing prices and credit developed in Section 7.1, where we condition on the supply side of the housing market. In Section 7.2, we augment the subsystem with a small model for the supply side of the Norwegian housing market. This model is simply taken from an existing model for the Norwegian economy, i.e. the Statistics Norway forecasting model KVARTS, see Appendix A for details. As will become evident in the preceding subsections, including the supply side dampens the long run impact of shocks, as construction activity responds to changes in housing prices.

7.1 Dynamic multipliers: the baseline model

The first set of simulations we perform are based on the subsystem of housing prices and credit presented in Section 6. All simulations are conducted using 1000 stochastic Monte Carlo replications and 95 percent simulated confidence intervals (dotted red lines) are reported along with the simulated response path (solid blue lines). The dynamic effects of a permanent increase in the growth of credit and housing prices are shown in Figure 2 and 3, respectively. The figures display the impact on the growth rates as well as on real housing prices and the stock of real household debt.

Figure 2: Baseline model dynamic multipliers of a shock to credit growth of 1 percentage point

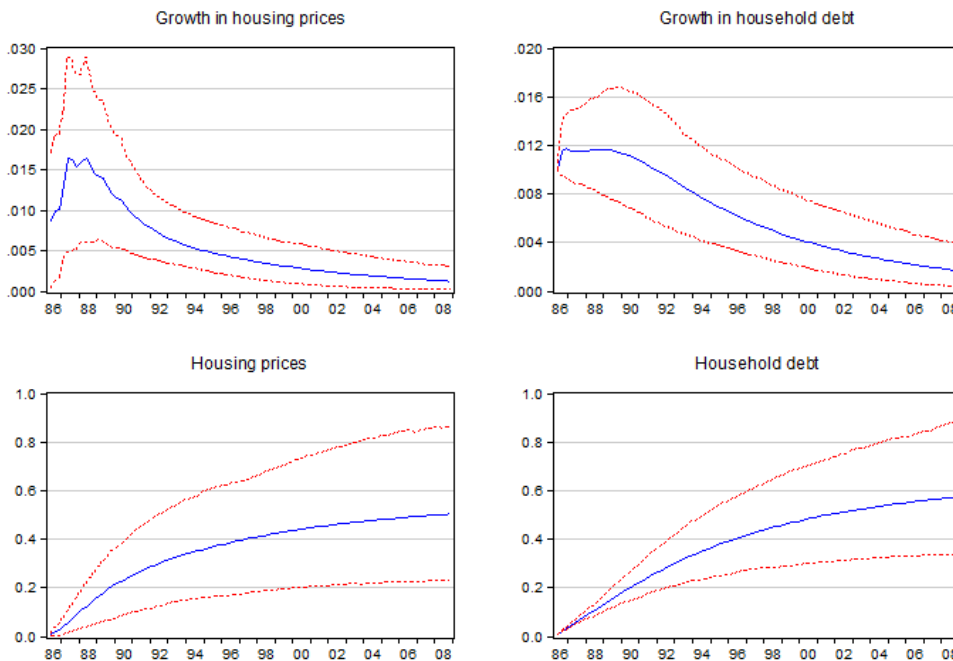
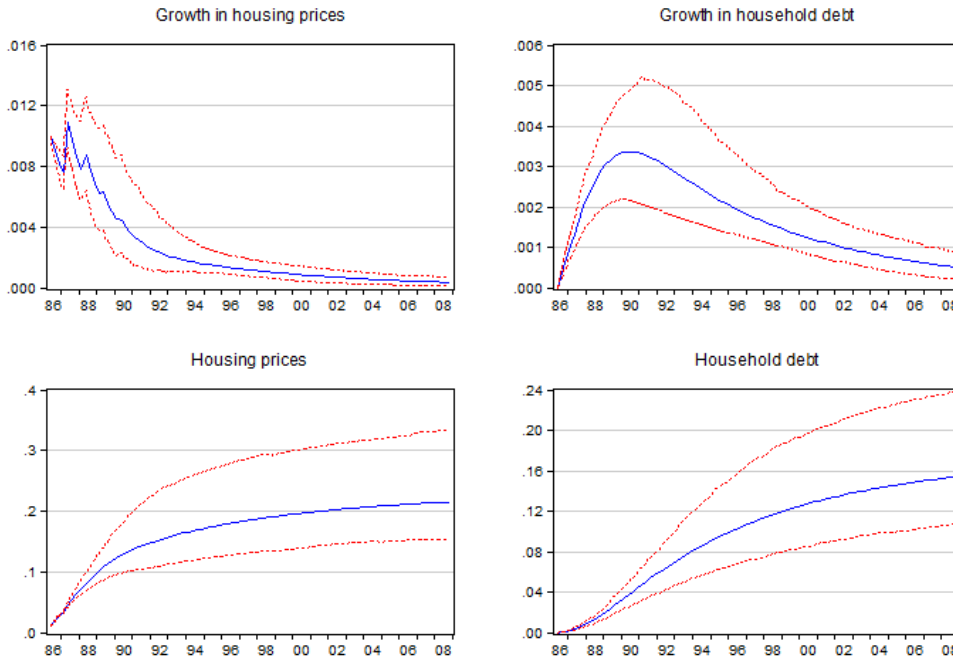


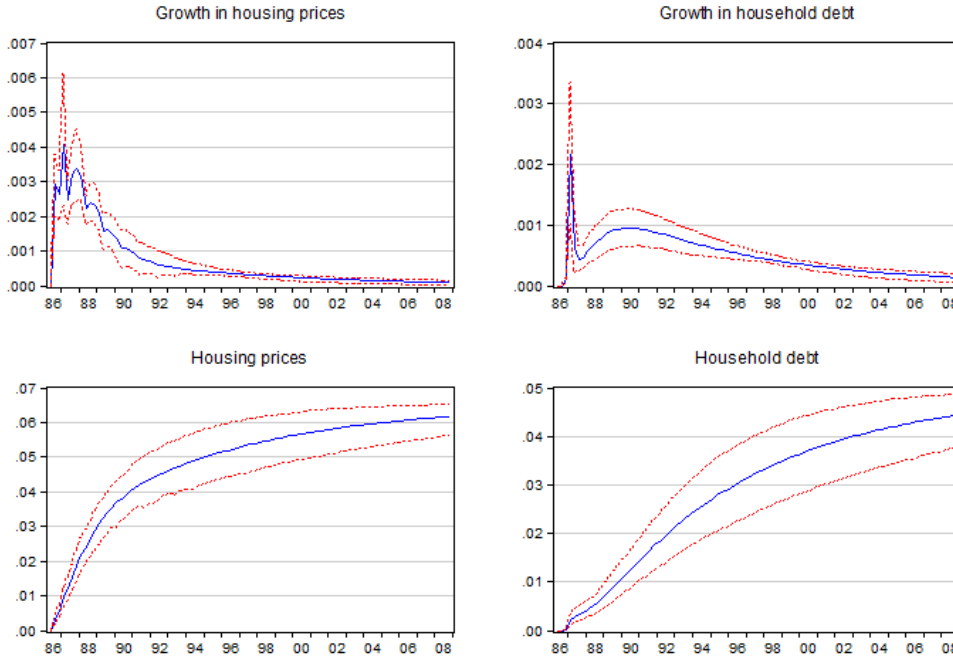
Figure 3: Baseline model dynamic multipliers of a shock to housing price growth of 1 percentage point



The figures show that an exogenous shock in one of the markets is propagated and amplified through an endogenous feedback mechanism. Figure 2 shows that a positive exogenous shock in the credit growth by one percentage point will increase housing price growth by 0.86 percentage points at the time of the shock, which equals the instantaneous impact on housing price growth in Table 6. The increase in housing prices leads to a further increase in credit growth in the subsequent period, as the collateral value has increased. This again induces further growth in housing prices and credit in a process that continues for about two years before the error correction term dominates and the effect of the shock gradually dissipates. In the long run there is of course no change in neither of the growth rates, but we see that the levels of both variables have stabilized at a higher level in accordance with the finding of a long run interaction between housing prices and credit in Section 5. Shocking housing price growth (see Figure 3) yields qualitative effects that are similar to the above described effects, and will of course not change any of the growth rates in the long run.

A shock to one of the exogenous variables in the system will have similar effects as is shown in Figure 4. A one percent increase in disposable income will lead to a growth in both housing prices and credit, which is reinforced by the feedback between the two variables. The dynamic process clearly indicates that the relationship between housing prices and credit is mutually self-reinforcing. First, a higher income leads to increased property valuations, which raises the value of the collateral. This spills over to the credit market, stimulating housing prices further, and so on. As the cumulative multipliers illustrate, both the growth in housing prices and credit continue to grow before the growth rates eventually return to zero. This has of course lead to a new equilibrium price level and a higher fundamental value

Figure 4: Baseline model dynamic multipliers of an increase in real disposable household income by 1 percent



for the credit variable, as seen from the lower part of the figure. An increase in disposable income, which is one of the long run determinants of housing prices, will change housing prices and credit period after period until they have adjusted to their new long run equilibrium level.

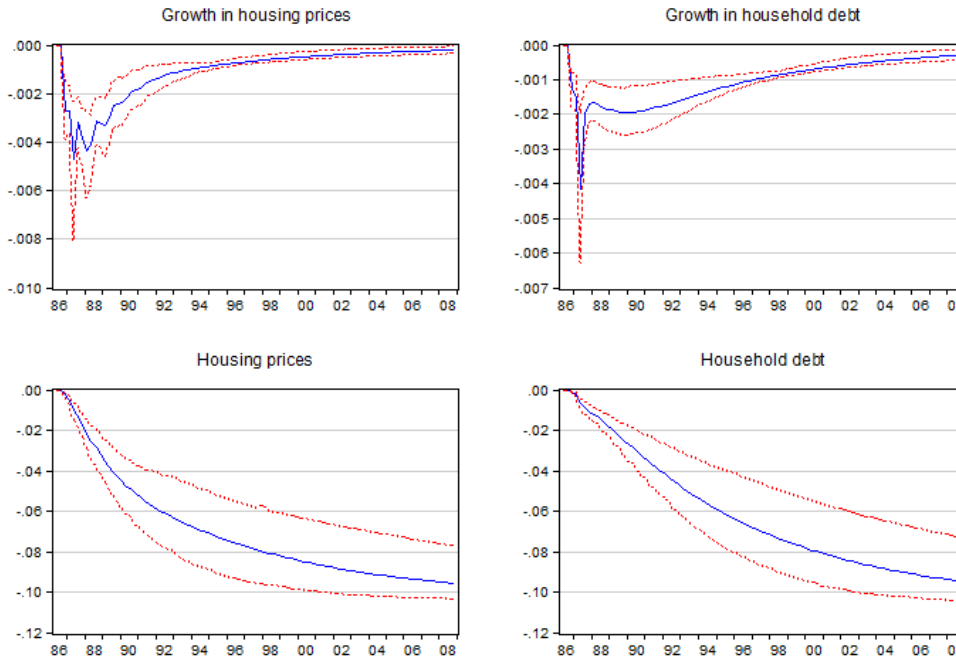
Figure 5 shows the simulated responses to one percentage point increase in the real interest rate. This reduces both housing prices and credit growth in the short run. In the long run both housing prices and household debt converge to new and lower equilibrium levels (lower part of the figure), which shows that the model implies interest rates effects on housing prices even though the interest rate does not enter the short nor the long run equations for housing prices directly.

7.2 Dynamic multipliers: an extended model

In this section we augment the core model above with a small model for the supply side of the housing market. These equations are lifted out of the macroeconomic forecasting model KVARTS, which is an operative and relevant model for the Norwegian economy. The supply side model captures the feedback from housing prices to the investments in new houses, which again affects the housing stock and therefore is expected to dampen the dynamic effects found in the previous subsection. The housing supply model is reestimated on our sample and a brief description of the supply side model along with the estimated coefficients are given in Appendix A. Figure 6 and Figure 7 illustrate the dynamic impact of a one percentage point increase in credit growth and housing price growth when the supply side is taken into account.

Though the short run effects are very similar to those for the baseline model,

Figure 5: Baseline model dynamic multipliers of a shock to the interest rate of 1 percentage point



we see that the effects of the shocks on the growth rates die off more quickly when taking into account that investment activity responds to changes in housing prices. In addition we see that the long run impact on housing prices and credit (the lower part of the figures) is much reduced when the supply side is included. The short run effects are almost unchanged as it takes time from new investments are initiated until the actual supply of houses increases. In the long run, we see the expected convergence to a new equilibrium with higher housing prices and a greater housing stock.

In Figure 8, we have graphed the simulated responses when we increase household disposable income by 1 percent. Again, it is clear that including the supply side dampens the effects relative to those reported in the previous section. In the long run we find that housing prices have increased by 0.05 percent, which is half of the initial increase in income. Household debt is found to increase by 1 percent, meaning that in the long run effect on debt will equal the initial shock to income.

The final figure (Figure 9) shows the effect of an increase in the real interest rate of one percentage point when we consider the extended model. Again, the short run response is similar to that in the baseline model, while the long run effect is much reduced. It should be noted that the disposable income variable includes net interest rate income, which is negative on aggregate for the households. Thus, if we had used a larger model, where also disposable income had been modelled, the simulated interest rate effect would be stronger.

Figure 6: Dynamic multipliers of a shock to credit growth of 1 percentage point in the extended model.

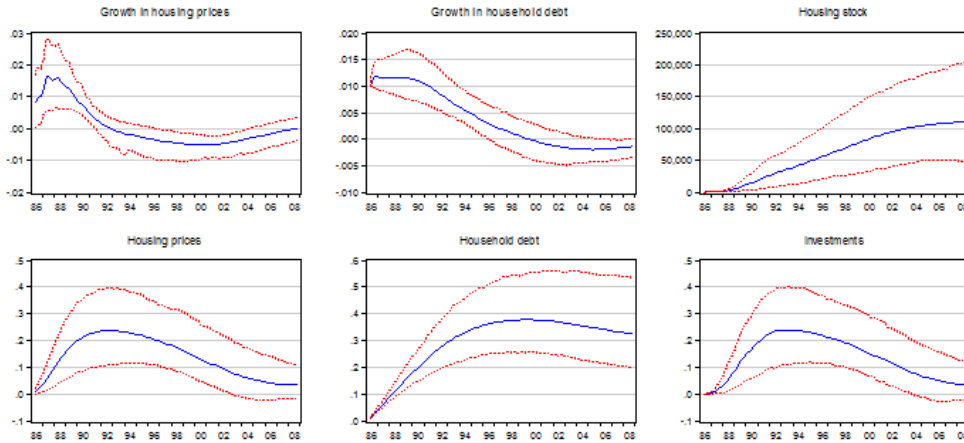
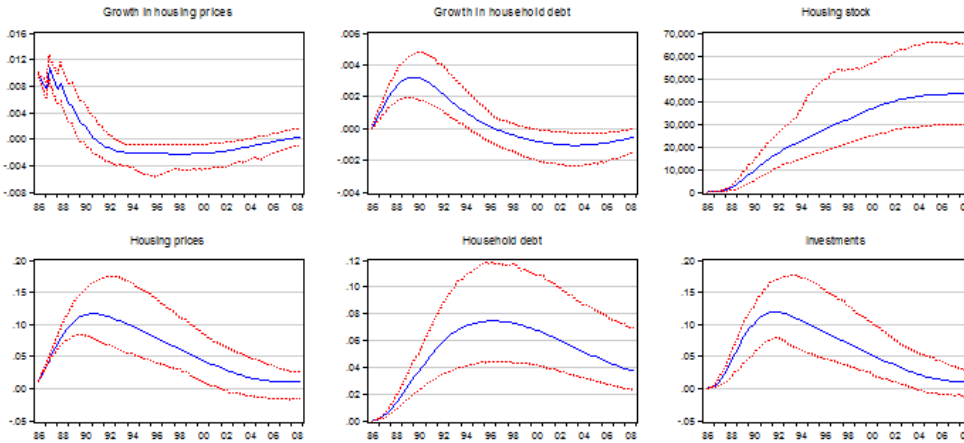


Figure 7: Dynamic multipliers of a shock to housing price growth of 1 percentage point in the extended model.



8 Conclusions

In this paper we first show that the cointegration analysis supports two long run relationships: one for housing prices and one for household debt. Also, household income can be considered weakly exogeneous with respect to the long run parameters. We find that housing prices depend on household borrowing, real disposable income and the housing stock in the long run, whereas real household debt is driven by the value of housing capital (housing prices times the housing stock), the real interest rate and the housing turnover. Housing prices and household debt are mutually dependent as both appear in the long run equation for the other. This suggests that there are feedback effects between the two in the long run. That said, housing prices are equilibrium correcting to deviations from both long run equations, whereas household debt adjusts only to disequilibria in the credit market.

Second, we embed the long run equations from the cointegration analysis in a simultaneous system explaining the changes in housing prices and debt, following a general to specific strategy. The equations are estimated simultaneously by full

Figure 8: Dynamic multipliers of an increase in real disposable household income of 1 percent in the extended model.

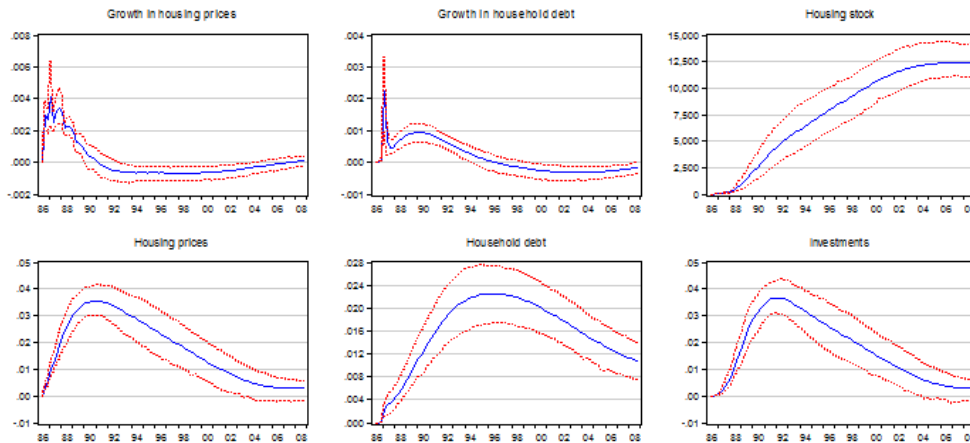
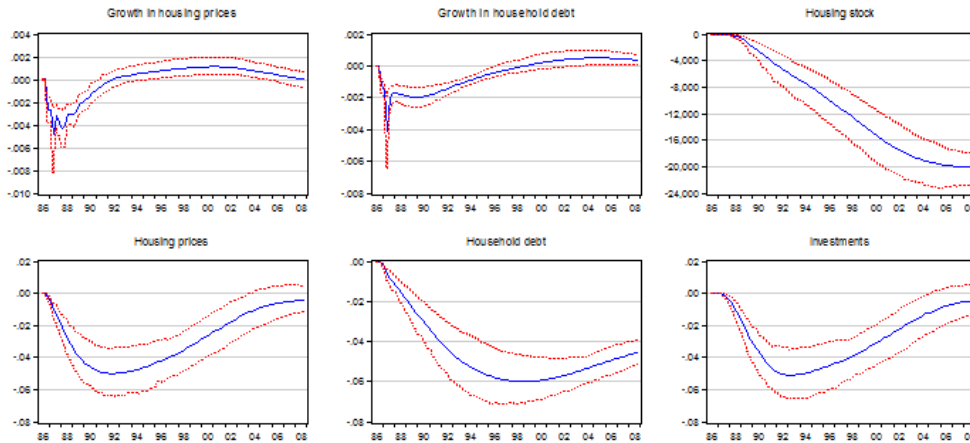


Figure 9: Dynamic multipliers of an increase in the real interest rate of 1 percentage point in the extended model



information maximum likelihood methods and insignificant variables are removed stepwise from the two equations. The estimation results suggest that the credit aggregate is important for housing price dynamics, but that housing prices only affect household borrowing through the error correction term.

Third, a consumer confidence indicator measuring households' expectations concerning future developments in their own economy as well as the Norwegian macro economy are incorporated into our framework. This variable explicitly picks up expectations about future economic conditions and is shown to enter significantly in the housing price equation in the short run.

Finally, the analysis of the dynamic multipliers provides clear evidence for the existence of a credit-housing price spiral in Norway. Higher housing prices result in higher credit growth due to collateral effects, which again spurs housing price growth and so on, showing that there indeed is a financial accelerator at work. The inclusion of the supply side dampens the dynamic responses of housing prices and credit to all shocks considered here.

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References

- Acharia, V. V. and P. Schnabl (2009). How banks played the leverage game. In Acharia, V. V. and M. Richardson (eds.), *Restoring Financial Stability: How to Repair a Broken System*, chap. 2, 83–100. Wiley, Hoboken, New Jersey.
- Akram, Q. F., G. Bårdsen and Ø. Eitrheim (2006). Monetary policy and asset prices: To respond or not? *International Journal of Finance & Economics*, 11, 279–292.
- Akram, Q. F., G. Bårdsen and K.-G. Lindquist (2007). Pursuing financial stability under an inflation-targeting regime. *Annals of Finance*, 3, 131–153.
- Andersen, H. (2011). Procyclical implications of Basel II: Can the cyclicity of capital requirements be contained? *Journal of Financial Stability*, 7, 138–154.
- Bårdsen, G., Ø. Eitrheim, E. S. Jansen and R. Nymoen (2005). *The Econometrics of Macroeconomic Modelling*. Oxford University Press, Oxford.
- Bårdsen, G., E. S. Jansen and R. Nymoen (2003). Econometric Inflation Targeting. *Econometrics Journal*, 6, 429–460.
- Berlinghieri, L. (2010). *Essays on House Price Fluctuations in the U.S.*. Ph.D. thesis, University of Washington, Seattle, USA.
- Bernanke, B. S. and M. Gertler (1989). Agency costs, net worth, and business fluctuations. *American Economic Review*, 79(1), 14–31.
- Bernanke, B. S. and M. Gertler (1995). Inside the Black Box: The Credit Channel of Monetary Policy Transmission. *The Journal of Economic Perspectives*, 9(4), 27–48.
- Bernanke, B. S., M. Gertler and S. Gilchrist (1999). The financial accelerator in a quantitative business cycle framework. In Taylor, J. B. and M. Woodford (eds.), *Handbook of Macroeconomics, volume 1*. North-Holland, Amsterdam.
- Borio, C., N. Kennedy and S. Prowse (1994). Exploring aggregate asset price fluctuations across countries. BIS Economic Papers 40, Bank of International Settlements, Basel.

- Brissimis, S. N. and T. Vlassopoulos (2009). The Interaction between Mortgage Financing and Housing Prices in Greece. *Journal of Real Estate Economics*, 39, 146–164.
- Dickey, D. A. and W. A. Fuller (1979). Distribution of the Estimates for Autoregressive Time Series with a Unit Root. *Journal of the American Statistical Association*, 74, 427–431.
- Doornik, J. A. (2003). Asymptotic tables for cointegration tests based on the Gamma-distribution approximation. Unpublished note, Nuffield College, Oxford.
- Doornik, J. A. (2009). Autometrics. In Castle, J. L. and N. Shephard (eds.), *The Methodology and Practice of Econometrics*, 88–121. Oxford University Press, Oxford.
- Doornik, J. A. and D. F. Hendry (2009a). *Empirical Econometric Modelling Using PcGive 13. Volume 1*. Timberlake Consultants, London.
- Doornik, J. A. and D. F. Hendry (2009b). *Modelling Dynamic Systems Using PcGive 13. Volume 2*. Timberlake Consultants, London.
- Duca, J. V., J. Muellbauer and A. Murphy (2010). Housing markets and the financial crisis of 2007-2009: Lessons for the future. *Journal of Financial Stability*, 6, 203–217.
- Eika, T. and K. Moum (2005). Substantial petroleum wealth: Does monetary policy regime matter? In Glomsrød, S. and P. Osmundsen (eds.), *Petroleum Industry Regulation within Stable States*, chap. 5, 90–111. Ashgate, Aldershot.
- Engle, R. F. and C. W. J. Granger (1987). Co-Integration and Error Correction: Representation, Estimation and Testing. *Econometrica*, 55, 251–276.
- Fitzpatrick, T. and K. McQuinn (2007). House Prices and Mortgage Credit: Empirical Evidence for Ireland. *The Manchester School*, 75, 82–103.
- Gerlach, S. and W. Peng (2005). Bank Lending and Property Prices in Hong Kong. *Journal of Banking and Finance*, 29, 461–481.
- Gimeno, R. and C. Martínez-Carrascal (2010). The relationship between house prices and house purchase loans: The Spanish case. *Journal of Banking and Finance*, 34, 1849–1855.
- Girouard, N., M. Kennedy, P. van den Noord and C. André (2006). Recent House Price Developments: The Role of Fundamentals. Working Papers 475, OECD Economics Department.
- Goodhart, C. and B. Hofmann (2007). *House Prices & the Macroeconomy. Implications for Banking & Price Stability*. Oxford University Press, Oxford.
- Hammersland, R. and D. H. Jacobsen (2008). The Financial Accelerator: Evidence using a procedure of Structural Model Design. Discussion Paper 569, Statistics Norway.

- Hendry, D. F. (1984). Econometric Modelling of House Prices in the United Kingdom. In Hendry, D. F. and K. F. Wallis (eds.), *Econometrics and Quantitative Econometrics*, chap. 8, 211–252. Blackwell.
- Hofmann, B. (2003). Bank lending and property prices: Some international evidence. Tech. Rep. 22, The Hong Kong Institute for Monetary Research.
- Hofmann, B. (2004). The determinants of private sector credit in industrialised countries: Do property prices matter? *International Finance*, 7, 203–234.
- Hubbard, R. G. and C. J. Mayer (2009). The Mortgage Market Meltdown and House Prices. *The B.E. Journal of Economic Analysis & Policy*, 9.
- IMF (2009). Global financial stability report: responding to the financial crisis and measuring systemic risks. Global financial stability report, april 2009, International Monetary Fund.
- Jacobsen, D. H. and B. E. Naug (2004). What influences the growth of household debt? *Economic Bulletin*, 75(3), 103–111.
- Jacobsen, D. H. and B. E. Naug (2005). What drives house prices? *Economic Bulletin*, 76(1), 29–41.
- Johansen, S. (1988). Statistical analysis of cointegration vectors. *Journal of Economic Dynamics and Control*, 12, 231–254.
- Johansen, S. (1992). Cointegration in Partial Systems and the Efficiency of Single-Equation Analysis. *Journal of Econometrics*, 52, 389–402.
- Juselius, K. (2006). *The Cointegrated VAR Model: Methodology and Applications*. Oxford University Press.
- Kiyotaki, N. and J. Moore (1997). Credit Cycles. *Journal of Political Economy*, 105(2), 211–248.
- Koetter, M. and T. Poghosyan (2010). Real estate prices and bank stability. *Journal of Banking and Finance*, 34, 1129–1138.
- Krogh, T. S. H. (2010). Credit Regulations in Norway, 1970-2008. Report 37/2010, Statistics Norway.
- Kwiatkowski, D., P. C. B. Phillips, P. Schmidt and Y. Shin (1992). Testing the null hypothesis of stationarity against the alternative of a unit root. *Journal of Econometrics*, 54, 159–178.
- Malpezzi, S. (1999). A Simple Error Correction Model of House Prices. *Journal of Housing Economics*, 8(1), 27–62.
- McQuinn, K. (2004). A Model of the Irish Housing Sector. Research Technical Paper 1/RT/04, Central Bank and Financial Services Authority of Ireland.

- Meen, G. (1990). The Removal of Mortgage Market Constraints and the Implications for Econometric Modelling of UK House Prices. *Oxford Bulletin of Economics and Statistics*, 52(1), 1–23.
- Meen, G. (2001). *Modelling spatial housing markets : Theory, analysis, and policy*. Kluwer, Boston.
- Meen, G. (2002). The Time-Series Behavior of House Prices: A Transatlantic Divide? *Journal of Housing Economics*, 11(1), 1–23.
- Meen, G. and M. Andrew (1998). On the Aggregate Housing Market Implications of Labour Market Change. *Scottish Journal of Political Economy*, 45(4), 393–419.
- Muellbauer, J. and A. Murphy (1997). Booms and Busts in the UK Housing Market. *Economic Journal*, 107(445), 1701–1727.
- Muellbauer, J. and A. Murphy (2008). Housing market and the economy: the assessment. *Oxford Review of Economic Policy*, 24, 1–33.
- Oikarinen, E. (2009a). Household Borrowing and Metropolitan Housing Price Dynamics: Empirical Evidence from Helsinki. *Journal of Housing Economics*, 18(2), 126–139.
- Oikarinen, E. (2009b). Interaction between housing prices and household borrowing: The Finnish case. *Journal of Banking and Finance*, 33, 747–756.
- Pain, N. and P. Westaway (1997). Modelling structural change in the UK housing market: A comparison of alternative house price models. *Economic Modelling*, 14(4), 587–610.
- Phillips, P. C. B. (1987). Time Series Regression with a Unit Root. *Econometrica*, 55, 277–301.
- Phillips, P. C. B. and P. Perron (1988). Testing for a Unit Root in time Series Regression. *Biometrika*, 75, 335–346.
- Poterba, J. (1984). Tax subsidies to owner-occupied housing: an asset market approach. *Quarterly Journal of Economics*, 99, 729–752.
- Tobin, J. (1969). A General Equilibrium Approach To Monetary Theory. *Journal of Money, Credit and Banking*, 1(1), pp. 15–29.
- Vale, B. (2004). The Norwegian Banking Crisis. In Moe, T. G., J. A. Solheim and B. Vale (eds.), *The Norwegian Banking Crisis Occasional Papers 33*, chap. 1, 1–21. Norges Bank, Oslo.

A The Supply Side

The equations describing the supply side of the housing market in Section 7 are lifted out of the Statistics Norway quarterly forecasting model, KVARTS (Eika and Moum (2005)) and reestimated on the current sample (1986q2-2008q4). In KVARTS, the supply of housing is modelled by considering housing starts measured in square meters. Housing starts serve as a leading indicator for the development in housing investments, which eventually become new houses and add to the housing stock.

In a long run perspective, new housing starts are modeled according to the q-theory of investments, where a one percent increase in either housing prices or a one percent decrease in construction costs lead to a one percent increase in housing starts. This implies that a proportional increase in construction costs and housing prices will have no long run effect on the supply of new houses. Letting S denote housing starts, PJ denote real construction costs and PH denote real housing prices, the reestimated equation for housing starts is given by (absolute t-values reported under the point estimates).

$$\begin{aligned}
 \Delta \log S_t &= \underset{(4.90)}{0.41} \Delta \log S_{t-4} - \underset{(4.28)}{0.26} (\log S_{t-1} - \log PH_{t-1} - \log PJ_{t-1}) \\
 &\quad + \text{dummies} \\
 (12) \quad R^2 &= 0.77
 \end{aligned}$$

In addition to the equilibrium correction term, the model contains an autoregressive part as well as an impulse dummy for the second quarter of 2002 and a set of seasonal dummies for the first three quarters. The re-estimated coefficients are almost unchanged from the version used in KVARTS, which is reassuring.

Since it takes time for a newly started building project to get finished, it is assumed that a change in housing starts will lead to a flow of investments for several years. In KVARTS this adjustment is assumed to take 12 quarters and the relationship linking investments and housing starts is given by the following equation:

$$(13) \quad \Delta \log(IH) = \Delta \log(J) + \text{seasonals}$$

where IH denotes housing investments, which grow proportionally with a weighted average of housing starts over the last 12 quarters, J . Also the coefficients for the seasonal dummy variables in equation (13) are reestimated when we construct the model used for simulations in Section 7. The weighted average of housing starts is given by the following identity .

$$\begin{aligned}
 J &= 0.3124 * S_t + 0.2455 * S_{t-1} + 0.1672 * S_{t-2} + 0.1125 * S_{t-3} + 0.0702 * S_{t-4} \\
 &\quad + 0.0407 * S_{t-5} + 0.0235 * S_{t-6} + 0.0131 * S_{t-7} + 0.0074 * S_{t-8} + 0.0043 * S_{t-9} \\
 &\quad + 0.0021 * S_{t-10} + 0.009 * S_{t-11} + 0.002 * S_{t-12}
 \end{aligned}$$

Finally, the housing stock is determined by a law of motion of capital accumulation:

$$H_t = (1 - \delta)H_{t-1} + IH_t$$

where δ is the rate of depreciation of the housing stock. As is evident from this brief presentation of the supply side, the model used for simulation in Section 7 captures spill overs from housing prices to the construction sector, which, as shown in the simulation exercises, dampens the long run effect of shocks on housing prices and credit.

B Data definitions

All data are seasonally unadjusted and measured on a quarterly basis. Except for the interest rate and the consumer confidence indicator all variables are transformed to log scale in the empirical analysis. Variable definitions and a brief description of the data are listed below.

pc: The consumption deflator in the National Accounts. Source: Statistics Norway.

ph: Hedonic housing price index measuring average housing prices in Norway. The index is calculated on the basis of data on sales in the second hand market. Statistics Norway officially started publishing housing price data in 1992. Prior to 1992 an unofficial index based on similar sources and compiled at Statistics Norway is used. The housing price index is deflated by *pc*. Source: Statistics Norway.

d: Total amount of outstanding gross household debt. Deflated by *pc*. Source: Statistics Norway.

yh: Households' disposable income, excluding equity income. Deflated by *pc*. Source: Statistics Norway.

h: Real housing stock measured in fixed prices. Measures the total stock of housing in Norway and is calculated according to the perpetual inventory method. Source: Statistics Norway.

th: The housing turnover measures the number of housing transactions. Source: Statistics Norway.

E: The expectations variable is taken from TNS Gallup and can be seen as a consumer confidence indicator. It is based on a survey, where average score can range between -100 and 100 . In this paper we have normalized the variable to lie between -1 and 1 . The indicator measures households expectations concerning the state of the economy and the development in their personal economy. Source: TNS-Gallup.

i: Nominal interest rate paid by households on loans in private financial institutions. Source: Statistics Norway.

p: Consumer Price Index. Source: Statistics Norway.

π : Annual inflation rate ($\Delta_4 p$).

τ : Capital tax rate. After a tax reform in 1992 τ has been constant at 0.28 . Source: Statistics Norway.

R: Real after-tax interest rate ($i * (1 - \tau) - \pi$).

Variables used in Appendix A:

S: Housing starts (square meters). Source: Statistics Norway.

J: Weighted sum of housing starts (square meters).

IH: Investments in housing, measured at fixed prices. Source: Statistics Norway.

PJ: Price index for construction costs, deflated by *pc*. Source: Statistics Norway.

δ : rate of depreciation of the housing stock.

C Single equation specification search

In this appendix, we document the model obtained if we follow the “standard approach”, i.e. specifying each equation separately before estimating them as a system. Adopting a single equation approach one would take the system represented by equation (10) and (11) as a starting point. This approach precludes any formal treatment of identification, but may possibly give reasonable results if the simultaneity bias is not large. We have used the automated multipath search algorithm Autometrics (see Doornik (2009) and Doornik and Hendry (2009a)) to reduce the dimensionality of each equation. An obvious advantage with this algorithm is that it is very little path dependent as it does a multipath search. However, the benefit from this might be outweighed by the fact that it does not allow us to take care of the simultaneity from the onset by doing a full fledged system analysis at each step in the reduction process. The results from this single equation general to specific approach are documented in Table C.1 and Table C.2 for the housing price and credit equation, respectively.

Table C.1: Short run dynamics obtained by Autometrics for housing price equation^a

Variable	Coefficient	t-value
<i>Constant</i>	1.23	6.78
Δd	0.61	3.85
Δph_{t-4}	0.41	4.93
Δt_{t-3}	0.05	2.55
Δr_{t-4}	-0.38	2.06
ΔE_t	0.095	4.54
ΔE_{t-1}	0.096	4.40
ΔE_{t-2}	0.05	2.17
ecm_{t-1}^{ph}	-0.07	3.81
ecm_{t-1}^d	-0.14	6.80
<i>CSeasonal</i> _t	-0.006	0.496
<i>CSeasonal</i> _{t-1}	-0.007	0.65
<i>CSeasonal</i> _{t-2}	-0.009	0.999
σ	0.0141	
R^2	0.82	
<i>Adj.R</i> ²	0.80	
Diagnostics ^b	Test statistic	Value [p-value]
AR 1-5 test:	$F(5, 73) =$	0.4789 [0.7909]
ARCH 1-4 test:	$F(4, 83) =$	0.4462 [0.7749]
Normality test:	$\chi^2(2) =$	1.5603 [0.4583]
Hetero test:	$F(21, 69) =$	1.3658 [0.1672]
Estimation Method	OLS (Autometrics with p-value = 0.05)	
Sample	1986q2-2008q4	

^a Absolute t-values are reported.

^b See Doornik and Hendry (2009a).

The results in Table C.1 and Table C.2 reveal some differences as compared to our preferred model. We note that both variables enter contemporaneously in both

Table C.2: Short run dynamics obtained from Autometrics for the credit equation^a

Variable	Coefficient	t-value
<i>Constant</i>	-0.73	10.6
Δph_t	0.30	7.06
Δph_{t-4}	-0.12	2.64
Δy_{t-2}	-0.15	3.10
ΔE_{t-1}	-0.04	2.45
Δr_{t-3}	-0.24	2.34
ecm_{t-1}^{ph}	0.09	10.8
<i>CSeasonal</i> _t	-0.004	1.16
<i>CSeasonal</i> _{t-1}	-0.004	1.50
<i>CSeasonal</i> _{t-2}	-0.01	4.07
σ	0.009	
R^2	0.72	
<i>Adj.R</i> ²	0.69	
Diagnostics ^b	Test statistic	Value [p-value]
AR 1-5 test:	$F(5, 76) =$	1.4959 [0.2011]
ARCH 1-4 test:	$F(4, 83) =$	0.7501 [0.5608]
Normality test:	$\chi^2(2) =$	4.9864 [0.0826]
Hetero test:	$F(15, 75) =$	0.8092 [0.6641]
Estimation Method	OLS (Autometrics with p-value = 0.05)	
Sample	1986q2-2008q4	

^a Absolute t-values are reported.

^b See Doornik and Hendry (2009a).

equations. Also, we observe that the income variable and the expectations variable are both highly significant in the credit equation with negative signs, which are not plausible *a priori*. Let us now turn to the two equations when they are estimated simultaneously to take care of potential endogeneity problems. Results are displayed in Table C.3.

The credit equation remains almost unaltered, while the housing price equation changes dramatically. First of all, the credit variable which is positive and highly significant in the single equation model has now changed sign and is insignificant. Also, the loadings have changed. As a final check of this model, we will explore how the implied dynamics of the system to a permanent increase in real disposable income would be. We follow exactly the same set up as in section 7.1 and the dynamic multipliers are graphed in Figure 10.

Table C.3: System estimation of the specifications obtained by Autometrics (equation by equation)^a

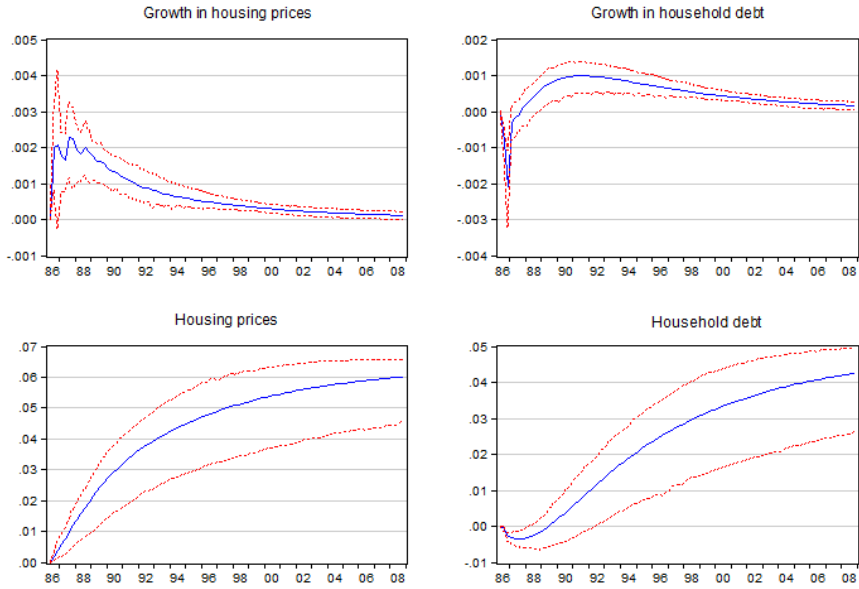
Variable	Real housing prices		Real household debt	
	Coefficient	t-value	Coefficient	t-value
Constant	1.00	3.78	-0.73	10.5
Δd_t	-0.26	0.49	-	-
Δph_t	-	-	0.32	5.50
Δph_{t-4}	0.36	3.65	-0.13	2.57
Δyh_{t-2}	-	-	-0.15	3.05
ΔE_t	0.12	3.88	-	-
ΔE_{t-1}	0.10	3.95	-0.04	2.48
ΔE_{t-2}	0.05	1.75	-	-
Δr_{t-3}	-	-	-0.24	2.37
Δr_{t-4}	-0.51	2.36	-	-
Δt_{t-3}	0.06	2.50	-	-
ECM_{t-1}^{ph}	-0.11	3.34	0.09	10.6
ECM_{t-1}^d	-0.10	3.85	-	-
Dummy, q1	-0.01	0.75	-0.005	1.26
Dummy, q2	-0.009	0.73	-0.004	1.55
Dummy, q3	-0.02	1.61	-0.01	4.07
Sargan	$\chi^2(43) =$	40.323 [0.5881]		
Log likelihood	567.99			
σ	0.016		0.0086	
Diagnostics ^b	Test statistic	Value [p-value]		
Vector SEM-AR 1-5 test:	$F(20, 138) =$	0.7944[0.7168]		
Vector Normality test:	$\chi^2(4) =$	4.7544[0.3134]		
Vector Hetero test:	$F(183, 81) =$	1.0260[0.4557]		
Estimation Method	FIML			
Sample	1986q2-2008q4			

^a Absolute t-values are reported.

^b See Doornik and Hendry (2009b).

Based on the dynamic multipliers from this alternative model, we see that it implies a negative response to household borrowing of an increase in income in the short run, which seems unreasonable from an economic point of view. Also, the credit effect on housing prices changes sign and turns out insignificant though it was positive and highly significant in the single equation case. Furthermore, we observe relative big changes in the loadings in the housing price equation. On this background we conclude that this model is inferior to the one from the simultaneous model design in Table 6.

Figure 10: The alternative model: Dynamic multipliers of a 1 percent increase in real disposable household income.



D Tables

Table D.1: Tests for the order of integration^a

Testing levels	ADF			PP			KPSS		
	$t - ADF$	5%	$Adj\ t - stat$	5%	LM	5%	5%	5%	Characteristics ^b
Variable	$t - ADF$	5%	$Adj\ t - stat$	5%	LM	5%	5%	5%	Characteristics ^b
ph	-2.37	-3.46	-1.32	-3.46	0.27	-3.46	0.27	0.146	t
d	-3.77	-3.46	-0.69	-3.46	0.27	-3.46	0.27	0.146	t
h	-2.76	-3.46	-0.78	-3.46	0.22	-3.46	0.22	0.146	t
ydp	-0.98	-3.46	-5.18	-3.46	0.31	-3.46	0.31	0.146	t
th ^c	-3.21	-3.46	-7.74	-3.46	0.14	-3.46	0.14	0.146	t
r	-3.58	-3.46	-3.5	-3.46	0.13	-3.46	0.13	0.146	t
E ^d	-1.80	-3.46	-2.15	-3.46	0.08	-3.46	0.08	0.146	t
Testing first differences									
Δph	-2.07	-2.89	-5.99	-2.89	0.25	-2.89	0.25	0.46	i
Δd	-1.77	-2.89	-5.35	-2.89	0.3	-2.89	0.3	0.46	i
Δh	-2.198	-2.89	-1.84	-2.89	0.29	-2.89	0.29	0.46	i
Δydp	-4.25	-2.89	-27.05	-2.89	0.44	-2.89	0.44	0.46	i
Δth	-8.71	-2.89	-21.91	-2.89	0.11	-2.89	0.11	0.46	i
Δr	-11.11	-2.89	-10.73	-2.89	.10	-2.89	.10	0.46	i
ΔE	-5.12	-2.89	-7.55	-2.89	0.28	-2.89	0.28	0.46	i
Testing second differences									
$\Delta^2 ph$	-4.62	-2.89	-	-	-	-	-	-	i
$\Delta^2 d$	-13.28	-2.89	-	-	-	-	-	-	i
$\Delta^2 h$	-2.548	-2.89	-11.41	-2.89	-	-2.89	-	-	i

^a While the PP and KPSS tests are performed in EViews, we run the ADF test in PcGive since this allow us to include seasonal dummies in the test regression. The variables for which we have included seasonal dummies in the test regressions are housing prices, disposable income and the turnover, as they all display a clear seasonal pattern.

^c The turnover is only collected from 1985q1, which means that with 8 lags in the ADF regression, the sample starts in 1987q2.

^b The different characteristics are: Including both trend and intercept (t) or only an intercept (i) in the test regression.

^d For the expectations variable we only have data for the period from 1992q3 and the variable is set to 0 in the period prior to this in the empirical analysis. For the tests for the order of integration, we use the period for which we have observations.

Table D.2: Augmented Dickey-Fueller tests for structural residuals^a

Levels					
Variable	t-ADF	5%-critical value	lags	trend	seasonal dummies
$\varepsilon_{\Delta ph}$	-8.846	-2.89	0	No	No
$\varepsilon_{\Delta d}$	-7.945	-2.89	1	No	No

^a We only have data for ecm_d from 1985q1 because it includes the turnover. The residuals from the short run system is tested over the period 1988q3-2008q4 since we only obtain data for the error correction terms from 1986q2.

Table D.3: Lag reduction for the exogenous variables in the unrestricted VAR ^a,

Lags	log likelihood	SC	HQ	AIC
5	869.13433	-14.194	-15.824	-16.926
4	866.47195	-14.433	-15.964	-16.999
3	860.07987	-14.590	-16.022	-16.991
2	857.56754	-14.832	-16.166	-17.067
1	854.16023	-15.055	-16.290	-17.124
0	845.28489	-15.157	-16.293	-17.061

Tests of lag reduction

5 to 4	F(6,112) =	0.55420 [0.7658]
5 to 3	F(12,148) =	0.96638 [0.4836]
5 to 2	F(18,158) =	0.83006 [0.6629]
5 to 1	F(24,163) =	0.81618 [0.7127]
5 to 0	F(30,165) =	1.0756 [0.3722]
4 to 3	F(6,116) =	1.4069 [0.2178]
4 to 2	F(12,153) =	0.98362 [0.4670]
4 to 1	F(18,164) =	0.91767 [0.5582]
4 to 0	F(24,168) =	1.2251 [0.2269]
3 to 2	F(6,120) =	0.55985 [0.7615]
3 to 1	F(12,159) =	0.66799 [0.7801]
3 to 0	F(18,170) =	1.1519 [0.3071]
2 to 1	F(6,124) =	0.78849 [0.5806]
2 to 0	F(12,164) =	1.4710 [0.1398]
1 to 0	F(6,128) =	2.1855[0.0485]*

Estimation period: 1986q2-2008q4

^a Endogenous variables: Real housing prices, real household debt and real disposable income. Restricted variables: Real interest rate after tax, housing turnover, housing stock and a linear trend. Unrestricted variables: Constant and seasonal dummies.